### CO3091 - Computational Intelligence and Software Engineering

Lecture 25



# Principles of Continuous Leandro L. Minku

## Overview

- Importance and motivation for continuous learning.
- What is continuous learning?
- Continuous learning algorithms.
- Adapting predictive models to changes.
- Evaluation of continuous learning algorithms.

### Importance and Motivation

- Many real world applications suffer changes over time. We say that they operate in changing environments. E.g.:
  - credit card approval,
  - prediction of electricity prices,
  - software effort estimation,
  - etc.



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## Importance and Motivation

- Many real world applications suffer changes over time. We say that they operate in changing environments. E.g.:
  - credit card approval,
  - prediction of electricity prices,
  - software effort estimation,
  - etc.
- These changes may affect the accuracy of predictive models.
  - A model that was good in the past may present bad accuracy after a change.

# What to do When There is a Change?



## Continuous Learning

- Many applications produce additional data over time.
- If we can learn additional data over time, we can improve our models based on such data.
- We can also use strategies to adapt our predictive models to changes.
- Continuous learning: algorithms that can learn additional data that arrive over time.
  - Lifelong learning.
  - Incremental learning.

## Supervised Learning

#### Training Data / Examples

x1 = age	x2 = salary	x3 = gender	 y = good/ bad payer
18	1000	female	 Good
30	900	male	 Bad
20	5000	female	 Good

Machine Learning



#### **Predictive Model**

New instance **x** for which we want to predict the output



Prediction

### Continuous Supervised Learning



Prediction

**Predictive Model** 

## Continuous Supervised Learning

Training and model usage co-occur.

The predictive model being used can be **updated** with new training examples.

## Types of Continuous Learning Algorithms

- Online machine learning algorithms:
  - Update predictive models whenever a new training example is received.
- Chunk-based learning algorithms:
  - Update predictive models when a whole chunk of training examples is received.

We will concentrate on online algorithms, because they can also be used when training examples arrive in chunks.

### • k-NN:

- Original algorithm can be used for continuous (online) learning.
- However, it may run into storage and efficiency problems as data become big.
- Needs strategies to adapt to changes.

### • Decision trees:

- Original algorithms need whole training set to decide on splits.
  - If you don't have all the training data beforehand, you need to re-build the model from scratch to learn new data.
  - Problem of using past + new training data:
    - Inefficient and does not allow us to deal with changes.
  - Problem of using only new data:
    - It can waste useful knowledge.

- Decision trees:
  - Other versions have been created for continuous (online) learning. E.g.: Hoeffding trees.
    - Associate training examples to nodes as they arrive.
    - Nodes with less than a minimum number of training examples are made into leaf nodes.
    - When a leaf node reaches a given number of examples, split this node.
    - Most of the continuous learning versions of decision trees still need some strategy to adapt to changes.

- Naive Bayes:
  - Can be used for continuous (online) learning quite efficiently.
  - Needs strategies to adapt to changes.

We've seen examples of algorithms that can be used to **update** predictive models with new training examples.

... but still need some strategy to **adapt to changes**.

# Why Are Strategies to Adapt to Changes Necessary?



[YouTube video posted by : <u>https://youtu.be/NXUUMLJbPCE</u>]

# Why Are Strategies to Adapt to Changes Necessary?

The coyote trained so much to catch the road runner, that now that he caught it he is struggling to adapt.

- A model is trained on new examples over time.
- When a change happens, many examples describing the situation before the change have been used.
- It would take many examples of the new situation to compensate for the old examples that were learnt.
  - Adaptation is slow.

# Error Why Are Strategies to Adapt to Changes Necessary?



## Dealing with Changes — Principles

Many approaches for dealing with changes are based on the following principles:

- Increase in error:
  - Error of a model is expected to reduce or stay constant over time if there is no change.
  - If the error of a model starts to increase, it is likely that there is a change causing this model to become inadequate.
- Building new model:
  - If current model(s) is(are) deemed inadequate for the current situation (increased error), create a new model to start learning the situation from scratch.

### Ensembles for Adapting to Changes

- What should we do with old models if we detect a change?
  - Some approaches will throw them away.
  - However, this may waste useful knowledge in case the new situation is somewhat similar to the old one, or if a past situation reoccurs.
- Ensembles of learning machines could be used as a way to keep old predictive models while still being able to adapt to changes.
- New predictive models can be added to the ensemble if changes are suspected or detected.
- Weights could be used to emphasise the models that best reflect the current situation.
  - E.g., weight could be proportional to the accuracy of the predictive model since the change was detected.

### Tracking a Model's Error Over Time

- Whenever a new training example arrives, we can use it to evaluate the predictive model before using it for training.
- This gives us an idea of how well the predictive model is performing as time passes.



### Examples of Error Functions

#### Classification error:

- Given a data set D with examples  $(\mathbf{x}_i, y_i)$ ,  $1 \le i \le n$ .
- The actual output (target) for  $\mathbf{x}_i$  is  $\mathbf{y}_i$ .
- The prediction given by a classification model to  $\mathbf{x}_i$  is  $\mathbf{y}_i^2$ .
- y<sub>i</sub> and y<sub>i</sub>' are categorical values.

Classification error =

$$\frac{1}{n} \sum_{i=1}^{n} (\mathbf{y}_{i} \neq \mathbf{y}_{i})$$

### Examples of Error Functions

- Mean Squared Error (MSE):
  - Given a data set D with examples  $(\mathbf{x}_i, y_i)$ ,  $1 \le i \le n$ .
  - The actual output (target) for  $\mathbf{x}_i$  is  $\mathbf{y}_i$ .
  - The prediction given by a regression model to  $\mathbf{x}_i$  is  $\mathbf{y}_i$ .
  - y<sub>i</sub> and y<sub>i</sub>' are numerical values.

MSE = 
$$\frac{1}{n} \sum_{i=1}^{n} (y_i - y_i)^2$$

### First Problem of Error Functions

• These error functions need to know the errors on all examples in order to compute the error.

Classification error = 
$$\frac{1}{n} \sum_{i=1}^{n} (y_i \neq y_i')$$
 MSE =  $\frac{1}{n} \sum_{i=1}^{n} (y_i - y_i')^2$ 

- This would mean that we would need to store all these errors.
- If there is a lot of data, we will run into storage issues.
- But... we can re-write these equations to update the error whenever a new prediction is made.

### Calculating Error in an Online Way

- The notation for the example iterator is typically t instead of i: (xt,yt)
- Classification error:

Classification error<sub>t</sub> = 
$$\begin{cases} (y_t \neq y_t') & \text{if } t=1 \\ \frac{t-1}{t} & \text{classification error}_{t-1} + \frac{1}{t} & (y_t \neq y_t') & \text{if } t>1 \end{cases}$$

Each example contributes equally to the error.

We have seen t examples so far.

Weight given to a single example:  $\frac{1}{t}$ Weight given to t - 1 examples:  $\frac{t-1}{t}$ 

### Calculating Error in an Online Way

• Classification error:

Classification error<sub>t</sub> = 
$$\begin{cases} (y_t \neq y_t') & \text{if } t=1 \\ \frac{t-1}{t} & \text{classification error}_{t-1} + \frac{1}{t} & (y_t \neq y_t') & \text{if } t>1 \end{cases}$$

• Mean Squared Error (MSE):

$$MSE_{t} = \begin{cases} (y_{t} - y_{t})^{2} & \text{if } t = 1 \\ \frac{t - 1}{t} & MSE_{t-1} + \frac{1}{t} & (y_{t} - y_{t})^{2} & \text{if } t > 1 \end{cases}$$



Calculate the classification error using the original classification error function and the online classification error function for the following examples and corresponding predictions:

- $y_1 = false, y_1' = true$
- $y_2 = false, y_2' = false$
- $y_3 = true, y_3' = false$

### Second Problem of Error Functions

- Equal importance is given to all training examples.
  - Past examples are given the same importance as more recent ones.
- If we want to find out how well a model is doing currently, we need to modify the equations.

### Exponential Decay Error Functions

• Classification error:

Classification error<sub>t</sub> = 
$$\begin{cases} (y_t \neq y_t') & \text{if } t=1 \\ \frac{t-1}{t} & \text{classification error}_{t-1} + \frac{1}{t} & (y_t \neq y_t') & \text{if } t>1 \end{cases}$$

• Mean Squared Error (MSE):

$$MSE_{t} = \begin{cases} (y_{t} - y_{t}')^{2} & \text{if } t = 1 \\ \frac{t - 1}{t} & MSE_{t-1} + \frac{1}{t} & (y_{t} - y_{t}')^{2} & \text{if } t > 1 \end{cases}$$

### Exponential Decay Error Functions

• Classification error with exponential decay:

Classification error<sub>t</sub> = 
$$\begin{cases} (y_t \neq y_t') & \text{if } t=1 \\ \mathbf{\eta} \text{ classification error}_{t-1} + (\mathbf{1} - \mathbf{\eta}) (y_t \neq y_t') & \text{if } t>1 \end{cases}$$

• Mean Squared Error (MSE) with exponential decay:

$$MSE_{t} = \begin{cases} (y_{t} - y_{t}')^{2} & \text{if } t = 1 \\ \eta & MSE_{t-1} + (1 - \eta) (y_{t} - y_{t}')^{2} & \text{if } t > 1 \end{cases}$$

 $\eta$ ,  $0 < \eta < 1$ , is a weight representing the importance of the past

## Further Reading

#### **Issues in Evaluation of Stream Learning Algorithms**

João Gama, Raquel Sebastião, Pedro Pereira Rodrigues

Proceedings of the 15th ACM SIGKDD international conference on Knowledge discovery and data mining

Pages 329-338

http://readinglists.le.ac.uk/lists/D888DC7C-0042-C4A3-5673-2DF8E4DFE225.html

http://dl.acm.org/citation.cfm?id=1557060